# Reducing the Impact of Selection Bias with Propensity Scores

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#### References I Use in Teaching A Lot

- Ahmed, A, Husain A, Love TE et al. (2006). "Heart failure, chronic diuretic use, and increase in mortality and hospitalization: An observational study using propensity scores." European Heart Journal 27: 1431-1439. [Uses propensity score matching combined with survival analyses to assess the impact of diuretics in HF patients. Incorporates formal sensitivity analysis and careful assessment of covariate balance, including the standardized differences plot.]
- Austin, P. C. and M. M. Mamdani (2006). "A comparison of propensity score methods: A case-study estimating the effectiveness of post-AMI statin use." Statistics in Medicine 25: 2084-2106. [Examines multiple approaches to propensity score modeling applied to the same data, including matching, stratification, covariate adjustment and weighting. A great "second paper" to read. Also looks at several ways of assessing residual confounding after stratification or matching.]
- 3. Connors, A. F., Jr., T. Speroff, et al. (1996). "The effectiveness of right heart catheterization in the initial care of critically ill patients. SUPPORT Investigators." *Jama 276*(11): 889-97. [Detailed PS matching and multivariate adjustment to account for selection bias, including sensitivity analysis state of the art in 1996.]
- D'Agostino, R. B., Jr. (1998). "Propensity Score Methods for Bias Reduction in the Comparison of a Treatment to a Non-Randomized Control Group." *Statistics in Medicine 17*: 2265-2281. [Very readable introduction to matching, stratification, and regression using PS, with useful examples. Excellent "first paper" to read.]
- 5. Gum, P. A., M. Thamilarasan, et al. (2001). "Aspirin Use and All-Cause Mortality Among Patients Being Evaluated for Known or Suspected Coronary Artery Disease: A Propensity Analysis." JAMA 286: 1187-1194. [PS Application: PS matching with non-proportional hazards model for survival analysis - results show an interesting impact of selection bias adjustment. Editorial by MJ Radford and JM Foody "How Do Observational Studies Expand the Evidence Base for Therapy?" pp. 1228-1230 - motivates observational studies vs RCT discussion, clustering, hierarchical models]
- 6. Joffe, M. M. and P. R. Rosenbaum (1999). "Invited commentary: propensity scores." *Am J Epidemiol 150*(4): 327-33. [Motivation for PS approaches geared to physician-epidemiologists, as well as a set of extensions to case/control studies and to dose/response issues]
- 7. Rosenbaum, P. R. (2002). <u>Observational Studies</u>. New York, Springer. [The major recent work on the subject of observational studies.]
- 8. Rosenbaum, P. R. (1991). "Discussing hidden bias in observational studies." *Ann Intern Med* 115: 901-5. [Some of the fundamentals of sensitivity analysis]
- 9. Rosenbaum, P. R. and D. B. Rubin (1985). "Constructing a Control Group Using Multivariate Matched Sampling Methods That Incorporate the Propensity Score." *The American Statistician 39*(1): 33-38. [Seminal paper on propensity matching]
- 10. Rubin, D. B. (1997). "Estimating Causal Effects from Large Data Sets Using Propensity Scores." *Ann Intern Med 127* (Part 2): 757-763. [A very readable introductory discussion of key propensity score issues.]
- 11. Rubin, D. B. (2001). "Using Propensity Scores to Help Design Observational Studies: Application to the Tobacco Litigation." *Health Services & Outcomes Research Methodology* 2: 169-188. [Detailed (yet readable) description of PS matching, subclassification, weighting, under high stakes. **Excellent "third paper" to read.**]

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#### Other References of Interest

- 12. Austin, P. C., M. M. Mamdani, et al. (2005). "The use of the propensity score for estimating treatment effects: Administrative versus clinical data." *Statistics in Medicine 24*: 1563-1578. [Stratifying on PS quintiles derived from administrative data did not also successfully balance clinical patient characteristics. Also, clinical data-based estimates of treatment effectiveness were attenuated compared to estimates from administrative data.]
- 13. Barker, F. G., II, S. Amin-Hanjani, et al. (2004). "Age-Dependent Differences in Short-Term Outcome after Surgical or Endovascular Treatment of Unruptured Intracranial Aneurysms in the United States, 1996-2000." *Neurosurgery 54*: 18-30. [PS Application: Stratified treatment effect analysis by propensity score quintile. PS for surgical treatment modeled for 1780 patients, using demographics, clinical characteristics, primary payer for care, type of admission, and hospital characteristics.]
- 14. Barnard, J., C. E. Frangakis, et al. (2003). "Principal Stratification Approach to Broken Randomized Experiments: A Case Study of School Choice Vouchers in New York City." *Journal of the American Statistical Association 98*(462): 299-323, including Comments and Rejoinder. [Application of the "principal stratification" framework to the problems of noncompliance and missing data in a randomized trial of school vouchers.]
- 15. Barsky, R., J. Bound, et al. (2002). "Accounting for the Black-White Wealth Gap: A Nonparametric Approach." *Journal of the American Statistical Association 97*(459): 663-673. [Interested in the effect of being black on "wealth-holding" in the black population. Approach involves reweighting the white wealth distribution based on a non-parametric estimate of the propensity score.]
- 16. Beddhu, S., M. H. Samore, et al. (2003). "Impact of timing of initiation of dialysis on mortality." *J Am Soc Nephrol* 14(9): 2305-12. [PS Application: 3 PS strata created and applied to a series of stratified Cox PH models. Some sensitivity analyses to account for the impact of censoring.]
- 17. Berg, G. D., A. Johnson, et al. (2003). "Clinical and Utilization Outcomes for a Pediatric and Adolescent Telephonic Asthma Care Support Program: A Propensity Score-Matched Cohort Study." *Dis Manage Health Outcomes* 11(11): 737-743. [PS Application: PS matching to find a suitable comparison cohort for 318 asthma care support program participants based on demographics, utilization, and procedures performed.]
- 18. Berger, V. W. (2005). "The reverse propensity score to detect selection bias and correct for baseline imbalances." *Statistics in Medicine 24*: 2777-2787. [Deals with the problem of potentially systematic baseline imbalance in individual blinded randomized trials. The reverse PS (defined within) permits detection of and correction for selection bias.]
- 19. Bingenheimer, J. B., R. T. Brennan, et al. (2005). "Firearm violence exposure and serious violent behavior." *Science 308*(5726): 1323-6. [PS Application: Examines longitudinal data on Chicago adolescents using a 12-way PS stratification (PS below 0.05 or above 0.75 then excluded) to look at relationship between exposure to firearm violence and subsequent perpetration of serious violence.]
- 20. Braitman, L. E. and P. R. Rosenbaum (2003). "Rare Outcomes, Common Treatments: Analytic Strategies Using Propensity Scores." *Ann Intern Med 137*(8): 693-696. [Propensity Scores: What They Are, Why They Work, and What They Can't Do. With subsequent Letter from Longstreth WT, Fahrenbruch CE and Koepsell TD "Propensity Scores for Rare Outcomes and Common Treatments" v. 139, pp. 152-153 which describes the use of PS to deal with imbalances observed in RCTs which need to be summarized with risk differences.]
- 21. Cannon, C. P., G. M. Gibson, et al. (2000). "Relationship of Symptom-Onset-to-Balloon Time and Door-to-Balloon Time With Mortality in Patients Undergoing Angioplasty for Acute Myocardial Infarction." *JAMA 283*: 2941-2947. [PS Application: PS used to address possible confounding no real detail, but led to somewhat reduced risk increase with

- increases in door-to-balloon time. With Editorial by Michael S. Lauer "Primary Angioplasty Time Is of the Essence" with several positive comments about the PS, also identifying need for lots of data and the fact that PS does nothing about hidden biases.]
- 22. Cepeda, M. S., R. Boston, et al. (2003). "Comparison of Logistic Regression versus Propensity Score When the Number of Events Is Low and There Are Multiple Confounders." *American Journal of Epidemiology 158*(3): 280-287. [Simulations comparing standard logistic regression for the outcome incorporating a group of covariates to standard logistic regression incorporating only the exposure variable and the quintiles of PS, based on the same covariates. Not that interesting a comparison, in my view. Conclusion was that # of events per confounder was the issue (small -> PS, >8 ->logistic regression).]
- 23. Christakis, N. A. and T. J. Iwashyna (2003). "The health impact of health care on families: a matched cohort study of hospice use by decedents and mortality outcomes in surviving, widowed spouses." *Soc Sci Med 57*(3): 465-75. [PS Application: PS matching used to match couples where decedent was in hospice to couples where decedent was not.]
- 24. Chu, J. H., S. J. Gange, et al. (2005). "Hormonal contraceptive use and the effectiveness of highly active antiretroviral therapy." *Am J Epidemiol 161*(9): 881-90. [PS Application: 1:1 PS match (actually they first stratified, found no mean differences within most strata in terms of PS, then selected matches at random from within the stratum, they used nearest-neighbor in the first stratum) of 77 hormonal contraceptive users to 77 non-users on the basis of demographics, clinical and lab characteristics, and prior use of health-care services.]
- 25. Clark, C. and A. R. Rich (2003). "Outcomes of homeless adults with mental illness in a housing program and in case management only." *Psychiatr Serv 54*(1): 78-83. [PS Application: PS subclassification to form high-, medium- and low-impairment groups based on psychiatric symptoms, alcohol, and drug use.]
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- 27. Cole, J. A., J. E. Loughlin, et al. (2002). "The effect of zanamivir treatment on influenza complications: a retrospective cohort study." *Clin Ther 24*(11): 1824-39. [PS Application: PS matching used to identify comparison groups with similar health service utilization, comorbidities and diagnosis (influenza) but no antiviral therapy.]
- 28. Copas, A. J. and V. T. Farewell (1998). "Dealing with Non-Ignorable Non-Response by Using an "Enthusiasm-To-Respond" Variable." *Journal of the Royal Statistical Society, Series A 161*(3): 385-396. [Development of a "propensity-to-respond" score based on an embarrassment assessment combined with demographics. Applied to an estimation of virginity from the National Survey of Sexual Attitudes and Lifestyles.]
- 29. Craske, M. G., D. Golinelli, et al. (2005). "Does the addition of cognitive behavioral therapy improve panic disorder treatment outcome relative to medication alone in the primary-care setting?" *Psychol Med 35*(11): 1645-54. [PS Application: PS Weighting, using a generalized boosted model built from confounders including study site, insurance, demographics, and various psychological and clinical measures. Only retained significant bivariate differences in PS model.]
- 30. Crown, W. H., R. L. Obenchain, et al. (1998). "The application of sample selection models to outcomes research: The case of evaluating the effects of antidepressant therapy on resource utilization." *Statistics in Medicine 17*: 1943-1958. [Illustration of sample selection models, which attempt to control hidden biases in treatment selection which are also correlated with the outcome of interest.]
- 31. D'Agostino, R., Jr. and D. B. Rubin (2000). "Estimating and using propensity scores with partially missing data." *Journal of the American Statistical Association* 95: 749-759.

- 32. D'Agostino, R. B., Jr., W. Lang, et al. (2001). "Examining the Impact of Missing Data on Propensity Score Estimation in Determining the Effectiveness of Self-Monitoring of Blood Glucose (SMBG)." *Health Services & Outcomes Research Methodology* 2: 291-315. [Assesses several PS-based and ANCOVA techniques for dealing with missing data in estimating the PS, and evaluating the outcome.]
- 33. Dehejia, R. H. (2004). "Practical propensity score matching: A reply to Smith and Todd." *J of Econometrics 125*: 355-364. [Discusses PS matching (1:1) in response to Smith and Todd's paper on matching for non-experimental data. Points out that a separate PS specification should be estimated for each comparison that you want to make, and that sensitivity analyses are very important, as well.]
- 34. Dehejia, R. H. and S. Wahba (2002). "Propensity Score-Matching Methods for Nonexperimental Causal Studies." *The Review of Economics and Statistics* 84(1): 151-161. [What to do when few controls are comparable to treated subjects. Uses data from the National Supported Work experiment and PS matching, comparing treatment effect estimates obtained from matching on the PS to benchmark results obtained from an experiment.]
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- 36. El-Bassel, N., L. Gilbert, et al. (2005). "Relationship between drug abuse and intimate partner violence: a longitudinal study among women receiving methadone." *Am J Public Health* 95(3): 465-70. [PS Application: Matching after multiple imputation using demographics, history of trauma, psychological distress, social support and HIV risks. Data were collected in three waves: confounders measured pre-treatment, outcomes post-treatment.]
- 37. Foody, J. M., C. R. Cole, et al. (2001). "A propensity analysis of cigarette smoking and mortality with consideration of the effects of alcohol." *Am J Cardiol* 87(6): 706-11. [PS Application: PS incorporated as a continuous variable in Cox PH models, after dropping largest and smallest quintiles.]
- 38. Foster, E. M. (2003). "Propensity Score Matching: An Illustrative Analysis of Dose Response." *Medical Care 41*(10): 1183-1192. [Use of PS methods for health services researchers, PS matching as a weighting for dealing with more than two exposure groups.]
- 39. Greenland, S. (2000). "An introduction to instrumental variables for epidemiologists." *International Journal of Epidemiology* 29: 722-729. [Introductory discussion of instrumental variables, for epidemiologists, with an application dealing with non-parametric adjustment for non-compliance in randomized trials.]
- 40. Greenland, S. and H. Morgenstern (2001). "Confounding in Health Research." *Annu. Rev. Public Health* 22: 189-212. [Describes confounding the context of a counterfactual model of causation source of bias in the estimation of causal effects.]
- 41. Gu, X. S. and P. R. Rosenbaum (1993). "Comparison of Multivariate Matching Methods: Structures, Distances, and Algorithms." *J of Computational and Graphical Statistics* 2(4): 405-420. [Optimal matching beats greedy (nearest available) matching, sometimes by quite a lot, in getting closely matched pairs, but not by much in terms of balancing the matched samples. Optimal full matching is substantially better than Optimal 1:k matching.]
- 42. Hahn, J. (1998). "On the Role of the Propensity Score in Efficient Semiparametric Estimation of Average Treatment Effects." *Econometrica* 66(2): 315-331.
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- 44. Harraf, F., A. K. Sharma, et al. (2002). "A multicentre observational study of presentation and early assessment of acute stroke." *BMJ 325*: 17-21.
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- 46. Heckman, J. J., H. Ichimura, et al. (1997). "Matching as an Econometric Evaluation Estimator: Evidence from Evaluating a Job Training Programme." *The Review of Economic Studies* 64(4): 605-654.
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- 49. Hill, A. B., D. Obrand, et al. (2000). "Hemispheric Stroke following Cardiac Surgery: A Case-Control Estimate of the Risk Resulting from Ipsilateral Asymptomatic Carotid Artery Stenosis." *Ann Vasc Surg 14*: 200-209. [PS Application: Case-control study with PS stratification discussion includes a meta-analysis of related prospective cohort studies.]
- 50. Hirano, K. and G. W. Imbens (2001). "Estimation of Causal Effects using Propensity Score Weighting: An Application to Data on Right Heart Catheterization." *Health Services & Outcomes Research Methodology* 2: 259-278.
- 51. Hirano, K., G. W. Imbens, et al. (2003). "Efficient Estimation of Average Treatment Effects Using the Estimated Propensity Score." *Econometrica* 71(4): 1161-1189.
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- 53. Holden, C. (2005). "Sociology. Controversial study suggests seeing gun violence promotes it." *Science* 308(5726): 1239-40. [Comment on Bingenheimer et al.]
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- 63. Katzan, I. L., R. D. Cebul, et al. (2003). "The effect of pneumonia on mortality among patients hospitalized for acute stroke." *Neurology* 60(4): 620-5. [PS Application: PS for pneumonia used for risk adjustment in logistic regression analyses.]
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- 65. Kennedy, J., H. Quan, et al. (2005). "Statins Are Associated With Better Outcomes After Endarterectomy in Symptomatic Patients." *Stroke 36*: 2072-2076.
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- Cardiomyopathy (A 25-Year Experience from the Duke Cardiovascular Disease Databank)." *Am J Cardiol 90*: 101-107.
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